In this work, we prove an analog of the fundamental theorem of Riemannian geometry for Born geometry, which describes a target space of a manifestly T-duality covariant effective string theory. We show that there exists a unique connection which preserves structures of the Born geometry and which is torsionless in a generalized sense. This resolves a fundamental ambiguity that is present in the double field theory formulation of effective string dynamics.